Current collapse in tunneling transport through benzene

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ABSTRACT

We investigate the electrical transport through a system of benzene coupled to metal electrodes by electron tunneling. Using electronic structure calculations, a semi-quantitative model for \( \pi \) electrons of the benzene is derived that includes general two-body interactions. After exact diagonalization of the benzene model the transport is computed using perturbation theory for weak electrode-benzene coupling (golden rule approximation). We include the effect of an applied electric field on the molecular states, as well as radiative relaxation. We predict a current collapse and strong negative differential conductance due to a “blocking” state when the electrode is coupled to the para-position of benzene. In contrast, for coupling to the meta-position, a series of steps in the \( I - V \) curve is found.

**Keywords**: molecular electronics, weak coupling mesoscopic transport, blocking state negative differential conductance

1 Introduction

Single molecule electronic devices offer exciting perspectives for further miniaturization of electronic circuits with a potentially large impact in applications. Several experiments have demonstrated the possibility to attach individual molecules to leads and to measure the electrical transport. [1]--[4] In contrast to single electron transistors (SETs) based on quantum dots [5] the electronic structure of molecular devices can be chemically designed for specific applications. When the molecule is coupled weakly to the electrodes, i.e. via electron tunneling, charging effects, semi-classically determined by the small capacitance of the molecule, become important. The interplay of charging effects with the specific structure of the molecular orbitals leads to nontrivial current voltage (\( I - V \)) characteristics [6], [7]. Very recent experiments demonstrated both Coulomb blockade and the Kondo effect in three terminal transport through a single molecular level [8], [9].

Using benzene as a prototypical example (see Fig ref:benz) we investigate novel effects that arise when transport through several competing electronic configurations becomes possible. We derive a semi-quantitative model for the conducting many-body states of the system from electronic structure calculations. For weak coupling to the electrode we compute transport within the golden rule approximation (sequential tunneling) and include screening of the applied electric field as well as radiative transitions between the electronic states of the molecule. We predict a current collapse in the \( I - V \) curve and strong negative differential conductance (NDC) due to the occurrence of a “blocking” state when the molecule is coupled to the electrode at the para-position. For coupling at the meta-position, the \( I - V \) curve displays a series of steps, but no NDC. We demonstrate how the specific spatial structure of the molecular orbitals qualitatively determines electronic transport. Finally, we discuss the limits of the model and the impact of disorder and symmetry breaking effects likely encountered in an experimental realization.

2 Model

2.1 Electronic Structure

To perform transport calculations in the weakly coupled regime, we extract an effective model from electronic structure calculations of the molecule. For benzene transport is assumed to be dominated by the \( \pi \)-electron system, but generalizations are straightforward. We first perform Hartree-Fock calculations in a suitable basis and then transform the Hamiltonian to the molecular orbital basis. We then integrate out the \( \sigma \) electrons of the system arriving at an effective interacting model Hamiltonian for the \( \pi \) electrons of the system in the presence of the atomic cores and the “frozen” density of
the $\sigma$ electrons:

$$\mathcal{H}_\sigma = \sum_{ij\sigma} e_{ij}\sigma_c^i \sigma_c^j + \sum_{ijk\sigma\sigma'} U_{ijkl} c_{ij\sigma}^\dagger c_{kl\sigma'} c_{ij\sigma} c_{kl\sigma'}$$ (1)

The second quantized operators $c_{ij\sigma}^\dagger$, $c_{ij\sigma}$ create/destroy electrons of spin $\sigma$ in orthogonalized Wannier-like orbitals centered at the carbon atoms. While this model neglects $\sigma$-$\pi$ mixing for certain excited states of the molecule [10], [11], its parameters account for the detailed electronic structure of the molecule. For the current work, we compute the model parameters only once, using an augmented double-zeta quality atomic natural orbital (ANO) basis set that was truncated to contain only one 2p-shell for each carbon. When applying a bias over the molecule this neglects the higher order effect of field screening by $\sigma$ electrons and its impact on the $\pi$ electrons. Note that there is no over-counting of interaction terms like in “interaction enhanced” density functional treatments in solid state physics [12], [13] that has to be corrected.

We find that the low-energy spectrum of benzene obtained from the diagonalization of the effective Hamiltonian operator eq. 1 compares favorably with the spectrum directly obtained from accurate multi-reference configuration interaction calculations [11], [14]. The remaining differences can be understood by the lack of $\sigma$-$\pi$ mixing and do not qualitatively affect the transport properties. The restriction to a pure $\pi$-electron system is more severe for the charged states, as discussed in some detail below.

To account for the effect of an external bias potential $V_{ext}$ on the electrons we include a term

$$\mathcal{H}_{bias} = e \sum_{ij\sigma\sigma'} V_{ij\sigma}^\text{ext} c_{ij\sigma}^\dagger c_{ij\sigma}$$ (2)

with $V_{ij\sigma}^\text{ext} = \int dr \Phi_i(r) V_{ext}(r) \Phi_j(r)$ and $V_{ext}(r) = (V_L + V_R)/2 - V_{bias}(r)$ in the Hamiltonian. $V_{bias}$ is the chemical potential in the left/right electrode, distances are measured from the center of the molecule. The matrix elements $V_{ij\sigma}^\text{ext}$ also result from the electronic structure calculation described above. We consider a bias $V_{bias} = V_L - V_R$ aligned with the transport direction ($x$-direction), unless otherwise specified. We measure distances from the center of the benzene. The parameter $L$ indicates the length over which the external bias falls off.

### 2.3 Transport Calculation

After diagonalization of the Hamiltonian we have the many-body eigenstates $|s\rangle$ with the corresponding energies $E_s$ and their total spin $S_s$. We use a Master equation approach [7] for the occupation probabilities $P_s$ in a stationary state. The transition rate $\Sigma_{ss'}$ from state $s'$ to $s$ is computed in perturbation theory using the golden rule. The “perturbation” is the coupling of the molecule to the leads

$$H_{\text{mol-leads}} = \left(\frac{\Gamma}{2\pi \rho_c}\right)^{1/2} \sum_{k\sigma} \left( c_{i\sigma}^a a_{k\sigma} + h.c. \right) ,$$ (3)

and (optionally) the coupling to electromagnetic fields (photons). $\Gamma$ is the coupling strength (in units of energy) of leads to the benzene and $\rho_c$ is the density of states of the electrons in the electrode (assumed constant). The operators $a_{k\sigma}$ and their hermitian conjugates destroy/create electrons with momentum $k$ and spin $\sigma$ in electrode $\alpha = \text{left}/\text{right}$. For simplicity, we assume that tunneling is only possible through two “contact” carbon atoms which we choose to be at the 1 and 4 (para) positions unless noted otherwise.

As we do not consider the leads microscopically, the coupling of molecule states $|s\rangle$ is determined by the overall coupling strength $\Gamma$ and the relative wave function amplitude of the state $|s\rangle$ at the coupling carbon site $l$. For the transition rates we have $\Sigma_{ss'} = \sum_{\alpha,\alpha' = \pm} \Sigma_{ss'}^{\alpha\alpha'}$ where $\Sigma_{ss'}^{\alpha\alpha'}$ is the tunneling rate to/from electrode $\alpha$ for creation ($\alpha = +$) or destruction ($\alpha = -$) of an electron on the molecule. We have

$$\Sigma_{ss'}^{\alpha\alpha'} = \Gamma f_\alpha (E_s - E_{s'}) \sum_{\sigma} \left| \sum_i <s|c_{i\sigma}^a|s'\rangle \right|^2 ,$$ (4)

and a corresponding equation for $\Sigma_{ss'}^{\alpha\alpha'}$ by replacing $f_\alpha \rightarrow 1 - f_\alpha$, where $f_\alpha$ is the Fermi function. When including relaxation by radiative transitions, we use the dipole approximation with dipole transition moments $d_{i,j} = \int dr \Phi_i(r) \Phi_j(r)$ obtained from the electronic structure calculations. The corresponding transition rates are

$$\Sigma_{ss'}^{\alpha\alpha'} = \frac{4e^2}{3\hbar^3} \langle s | \mathcal{S}^\text{ext} | s' \rangle \sum_{\sigma} \left| \sum_i <s|c_{i\sigma}^a|s'\rangle \right|^2$$

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where $N_b(E)$ denotes the equilibrium Bose function. Note that for emission $E_b - E_{b'}$ is negative, and $N_b(-|E|) = -(1 + N_b(|E|))$.

The total transition matrix $\Sigma_{g^g'}$ consists of blocks connecting $N$ and $N \pm 1$ electron states (tunneling processes) and blocks from the radiative transitions that do not change the electron number on the molecule. Taking only one member of the subspace of spin and energy degenerate states into account, the rank $r$ of the transition matrix is 1716. The stationary condition $\tilde{P}_s = 0$ can be written as $\sum s' A_{g^g'} \tilde{P}_{s'} = 0$ with the matrix $A_{g^g'} = \Sigma_{g^g'} - \sum s', \Sigma_{g^g} \delta_{g'^g}$. This implies that $A_{g^g'}$ has an eigenvector with zero eigenvalue, which is the wanted solution for $\tilde{P}_s$. Rather than computing this eigenvector by brute force, to speed up the calculation we make use of $\sum s \tilde{P}_s = 1$ to eliminate one row/column, thus reformulating the eigenvector problem into one of solving an inhomogeneous linear system of rank $r - 1$. Eventually, the current in the left and right electrode is calculated via $I_\alpha = e \sum_{g^g'} (\Sigma_{g^g} \tilde{P}_{g'} - \Sigma_{g^g} \tilde{P}_g)$.

In this paper, we consider symmetric bias only. Applying an asymmetric bias would effectively imply different coupling to the left and right leads and has been previously discussed [7]. Finally, we note that we must have $\Gamma \ll k_b T \approx 40 meV$ for perturbation theory to apply at room temperature $T$.

Figure 3: Sketch of the energetics and symmetry of the relevant neutral and anion states. At a left bias of 2.1 eV the antisymmetric blocking state becomes occupied via radiative relaxation. At 3.4 eV electrons can escape the blocking state via tunneling to the antisymmetric state of neutral benzene.

3 Results

To elucidate the impact of various effects on the current we have performed transport calculations with and without radiative transitions (relaxation) and with and without effect of the applied bias. On the left panel of Fig. 2 we present the $I - V$ curve obtained without the effect of the applied field (zero bias electronic structure). Without radiative relaxation (solid line) the $I - V$ curve consists of a series of steps of which only a few are well resolved on this scale. The first step is associated with the population of the first $\pi^*$ orbital of molecule (molecular charge $=-e$), an electron hops onto the lowest available level and then hops off again. At slightly larger bias, a transition of the anion to the first excited state of the neutral molecule becomes possible, resulting in a slight increase of the current. If the bias is sufficiently large this excited state may now accept another electron to populate higher excited states of the anion or low-lying states of the di-anion, resulting in a rapidly growing cascade of transitions between literally hundreds of states of the system. In the model considered here the growth of this cascade leads to quasi-ohmic behavior above 3.6 eV. In our calculation the first states of the di-anion become occupied at about 4.5 eV.

The inclusion of radiative transitions has a dramatic effect on the $I - V$ curve (dashed line). We observe a collapse of the current over a substantial range of the applied bias (2.1-3.4 eV). The reason for this collapse is the population of a “blocking” state in the cascade of transitions that becomes possible when excited states of the neutral molecule and anion become accessible. Above approximately 2.1 eV bias an excited state of the anion at about 5.6 eV (see Fig. 3), becomes partially populated in the transport cascade. This state can decay by photon emission to either a symmetric or an antisymmetric many body state (with respect to the plane through the transport axis and perpendicular to
the molecular plane) of the anion. In the bias range of the current collapse this state cannot decay by coupling to the leads, because the lowest neutral states are symmetric (see Fig. 3) and the tunneling preserves the symmetry. Since there are no further radiative transitions possible on the molecule, the rate equations contain no draining term from this state. As a result, in the stationary state, the probability of occupying the “blocking” state is unity and the current ceases to flow. At a larger bias (3.4 eV), the first escape channel opens, and the system can decay to the first antisymmetric excited state of the neutral molecule, which can then decay further by photon emission.

The above calculations simplify the illustration of the mechanism of NDC, because the energies of the participating states are independent of the applied bias. In the physical system the various states couple differently to the applied field. The solid line in the right panel of Fig. 2 shows the $I-V$ curve of the benzene with radiative relaxation and with the effect of the external potential applied parallel to the transport axis. We note a shift of the first step in the $I-V$ curve, which is due to differential screening effects between the ground state of the neutral molecule and the anion. At larger bias, the differential effects on all of the states in the cascade result in a significant renormalization of the $I-V$ curve. However, the current collapse still occurs, although the voltage window is reduced. The onset of quasi-ohmic behaviors occurs at higher voltage and a series of weak NDC effects occurs due to redistribution of occupation probabilities in favor of states with slightly smaller “transmission”.

If we couple the right electrode to the meta position of benzene (left panel, dash-dotted curve) we find no current collapse with or without radiative relaxation or bias effect. This can be readily understood by the fact that at the meta position the wave function of the formerly blocking state is non-vanishing and electrons can tunnel out to the right electrode. Consequently, we observe a series of current steps similar (but not identical) to the case of coupling to the para position without relaxation.

4 Discussion

In the above we have described transport in an idealized, though semi-quantitative, π-electron model of weakly coupled benzene and found a dramatic suppression of the current in a finite voltage window. The mechanism for this effect is the occupation of a so-called blocking state of the molecule, which cannot decay for symmetry reasons. There are a number of effects not explicitly considered here, e.g. symmetry breaking or transport through the σ-system, that influence the stability of this effect under experimental conditions. Their detailed discussion is beyond the scope of this summary, for details see [15], [16].

In weakly coupled molecules the concept of the “blocking” state suggests new opportunities for the design of single molecule electronic devices. In this investigation we have demonstrated how transport through several competing many-body states can result in strong NDC and current collapse over a significant voltage window. Our calculations predict the existence of this effect for a realistic molecule. Note that for $V_{bias}$ in the vicinity of the current peak, the application of a gate voltage $V_g$ may induce a large asymmetric change in the current, which would first rise and then drop again upon scanning of $V_g$ through a certain range. This behavior could be useful in various electronic devices.

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