

# A Surface-Potential-Based Compact Model of NMOSFET Gate Tunneling Current

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## ABSTRACT

This work presents a novel compact model for the gate tunneling current in n-channel MOSFET. The model is surface-potential based in both the channel and overlap regions. The Esaki-Tsu formulation is approximated to retain the essential physics without sacrificing the computational efficiency. Four parameters are sufficient to reproduce the bias and geometry dependence of the gate current.

**Keywords:** MOSFET, compact model, gate current, direct tunneling, current partition.

## 1 INTRODUCTION

Surface-potential-based approach provides significant advantages in the development of both the intrinsic [1] and extrinsic compact MOSFET models [2]. From the general point of view, it allows one to increase the physics content of the model and by doing so to reduce the total number of adjustable parameters. For example in this work four parameters are sufficient to reproduce complicated bias and geometry dependence of the gate current. The continued aggressive scaling of the gate oxide thickness ( $T_{ox}$ ) makes the accurate modeling of the gate tunneling current  $I_g$  an important aspect of the compact MOSFET model. This work presents a novel compact model of  $I_g$  which is valid in all regions of MOSFET operation and is surface-potential based in both the channel and the overlap regions. This approach is made practical by the recently developed analytical approximations for the surface potentials in both the channel [3] and the overlap regions [2]. As shown in Fig. 1 the total gate current is a sum of three components,  $I_{gsov}$  and  $I_{gdov}$  from the overlap regions and  $I_{gc}$  from the channel area. The physics-based description of the overlap regions is particularly important for the scaled devices. Indeed as explained in section 4, the overlap components dominate in the accumulation and

depletion regions and remain a significant fraction of  $I_g$  in inversion.

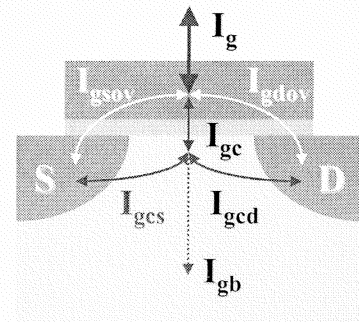


Figure 1: Gate tunneling current components.

## 2 GATE TUNNELING CURRENT DENSITY

In n-channel MOSFET, it has been shown that the dominant tunneling is between the conduction band in Si and the conduction band in polysilicon gate [5]. The tunneling current density [4]

$$J_g = qm^*k_B T / (2\pi^2\hbar^3) \int_0^\infty D(E)F(E)\lambda dE \quad (1)$$

where  $q$  is the absolute value of the electron charge,  $m^*$  is the effective electron mass in the direction perpendicular to the Si/SiO<sub>2</sub> interface,  $D(E)$  and  $F(E)$  are the transmission coefficient and the supply function as functions of the kinetic energy  $E$  in the direction of tunneling, respectively. The numerical integration inherent in (1) does not allow one to incorporate it directly into compact MOSFET models. Consequently in circuit applications it is common to use expressions significantly simpler than (1), which unfortunately do not include the supply function. This often produces some unphysical results which requires empirical fixes. In what follows, we present an alternative approach in which the integral in (1)

is approximated by assigning a single energy  $q\psi_t$  (cf. Fig. 2) to all tunneling electrons:

$$J_g \approx qm^*k_B^2T^2/(2\pi^2\hbar^3)D(\psi_t)F(\psi_t) \quad (2)$$

In WKB approximation

$$D(\psi_t) = \exp\left\{\frac{2T_{ox}}{\hbar}\sqrt{2qm^*\chi_{Bt}}[G_1 + G_2z_g(1 - G_3z_g)]\right\} \quad (3)$$

where  $\chi_{Bt} = \chi_B - \psi_t$ ,  $\chi_B$  is the conduction band offset at the Si/SiO<sub>2</sub> interface,  $z_g = |V_{ox}|/\chi_{Bt}$ , and  $V_{ox}$  is the position dependent oxide voltage. The numerical difference between (1) and (2) is absorbed by parameter  $G_1$  which controls the overall tunneling current level. Similarly, the uncertainty in  $m^*$  as well as the inaccuracy introduced by the WKB approximation are absorbed in the two remaining dimensionless model parameters, which control the slope ( $G_2$ ) and curvature ( $G_3$ ) of the  $\log I_g$  vs.  $V_{gs}$  characteristics. The fourth parameter is used to adjust  $\psi_t$  (cf. Fig. 2). The supply function is given by

$$F(\psi_t) = \ln\left\{\frac{1 + \exp[(\phi_s - \phi_n - \alpha_b - \psi_t)/\phi_t]}{1 + \exp[(\phi_s - V_{gb} - \alpha_b - \psi_t)/\phi_t]}\right\} \quad (4)$$

where  $\phi_s$  is the surface potential,  $\phi_n$  is the imref splitting,  $\alpha_b$  is the difference between the conduction band edge and the Fermi energy level in the Si bulk, and  $\phi_t = k_B T/q$  is the thermal voltage. The gate bias dependence of the supply function is shown in Fig. 2. Note also the physically meaningful result  $F(\psi_t) = 0$  and  $J_g = 0$  for  $V_{gb} = V_{ds} = 0$  (hence  $\phi_n = 0$ ) which obtains without any artificial multiplication factors often required in the some compact models of  $I_g$ .

### 3 GATE CURRENT PARTITION

The same expressions (2)-(4) are used to compute all the three components of the gate current ( $I_{gc}$ ,  $I_{gsov}$  and  $I_{gdov}$ ). In the overlap contributions,  $I_{gsov} = L_{ov}W_{eff}J_g$  and  $I_{gdov}$ , the overlap length  $L_{ov}$  is extracted from C-V data. As in [6,7], the tunneling current in the channel area

$$I_{gc} = W_{eff} \int_0^{L_{eff}} J_g dy \quad (5)$$

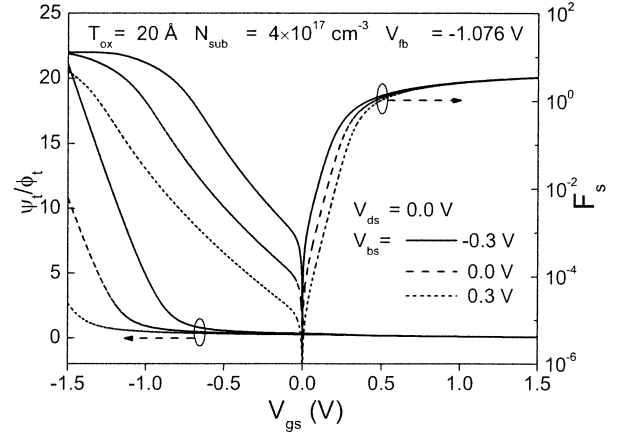


Figure 2: Gate bias dependence of the supply function.

is partitioned into the source and drain components following the theory developed in [6,7],  $I_{gcs} = I_{gc} - I_{gcd}$  and

$$I_{gcd} = (W_{eff}/L_{eff}) \int_0^{L_{eff}} J_g y dy \quad (6)$$

Using equation [1]

$$dy/d\phi_s = L_{eff}(q_i + \alpha_m\phi_t)/[(q_{im} + \alpha_m\phi_t)\phi] \quad (7)$$

the integrals can be evaluated in a closed form to obtain

$$I_{gc} = I_{gc0}[(1-b)\sinh(x)/x + b \cosh(x)] \quad (8)$$

and

$$I_{gcd} = \frac{I_{gc}}{2} - I_{gc0} \frac{\sinh(x)}{x} \left\{ A_g x - B_g \left[ \coth(x) - \frac{1}{x} \right] \right\} \quad (9)$$

In (7)-(9),  $q_{im}$  is the normalized inversion charge ( $q_i$ ) at the potential midpoint  $\phi_m$ ,  $\alpha_m$  is the symmetric linearization coefficient [1],  $I_{gc0} = WLJ_g(\phi_m)$ ,  $x = \phi/(2u_0)$ ,  $\phi$  is the surface potential difference along the channel,  $u_0 = 8\chi_{Bt}/\{3[1 + 2z_g(\phi_m)]\}$ ,  $b = u_0/(q_{im}/\alpha_m + \phi_t)$ ,  $A_g = (1 - 3b + 3b^2)/2$  and  $B_g = b(1 - b)/2$ . The partition of  $I_{gc}$  for different gate biases is illustrated in Fig. 3. In the accumulation region  $I_{gcs} = I_{gcd} = 0$ ,  $I_{gc}$  flows into the substrate and becomes a part of substrate current, ( $I_{gc} = I_{gb}$  in Fig. 1).

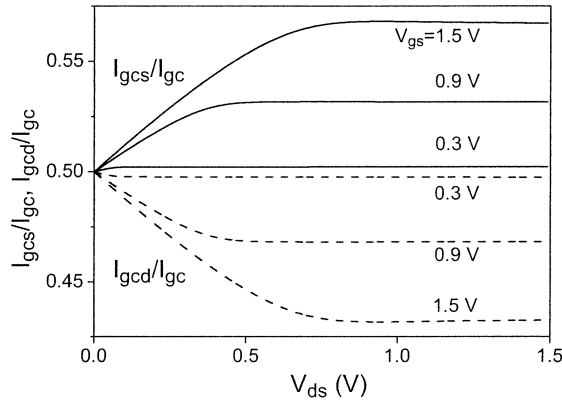


Figure 3: Partition of  $I_{gc}$  into source and drain components. Parameters are the same as in Fig. 3.

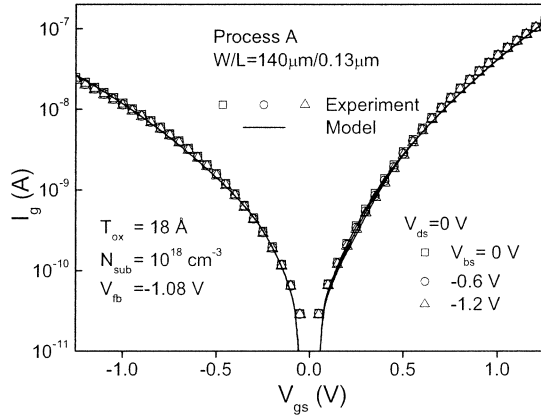


Figure 4: Experimental data for short-channel device by process A (symbols) and model calculations (lines).

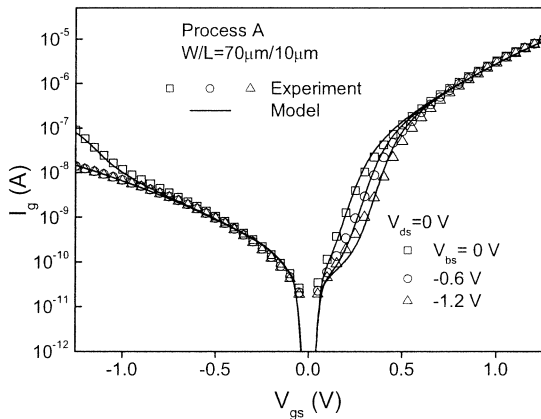


Figure 5: Experimental data for long-channel device by process A (symbols) and model calculations (lines).

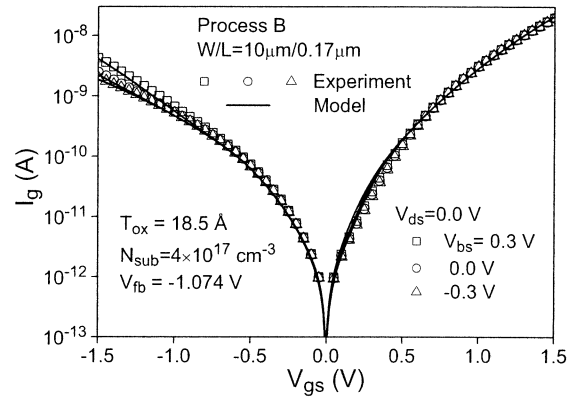


Figure 6: Experimental data for short-channel device by process B (symbols) and model calculations (lines).

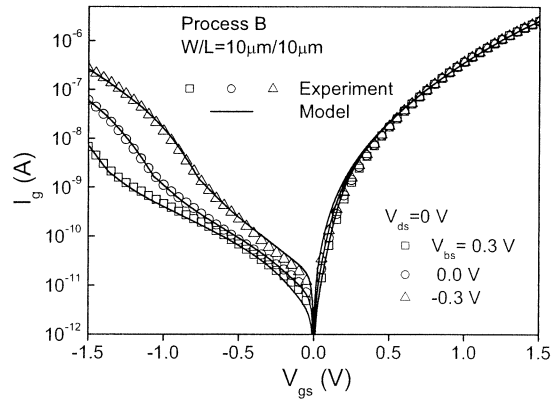


Figure 7: Experimental data for long-channel device by process B (symbols) and model calculations (lines).

## 4 RESULTS AND DISCUSSIONS

The accuracy of the new gate tunneling current model has been verified using experimental data for two advanced processes denoted as A and B. Typical results for  $V_{ds} = 0$  are shown in Figs. 4-7. The back bias dependence for  $I_g$  of the long-channel devices is stronger than that of the short-channel devices, in which the contribution of the overlap regions is significant for all  $V_{gs}$ . This is illustrated in Figs. 8 and 9, where  $I_g$  is decomposed into the contributions of the channel and overlap areas. In the inversion region of the long channel devices  $I_{gc}$  dominates and the back bias effect of  $I_g$  is significant. However, for short-channel devices,  $I_{gsov} + I_{gdov} \gg I_{gc}$  in the depletion region, and, since  $I_{gsov} + I_{gdov}$  is not affected by  $V_{bs}$ , neither is  $I_g$ . The drain bias dependence of  $I_g$  is

presented in Fig. 10. There are two physical mechanisms responsible for  $I_g(V_{ds})$  dependence. The gate current in the drain overlap region  $I_{gdov}$  is dependent on  $V_{ds}$ . Furthermore, the current in the channel area  $I_{gc}$  is also dependent on  $V_{ds}$  since  $V_{ds}$  controls the position dependence of the imref along the channel, which makes  $I_{gc}$  a decreasing function of  $V_{ds}$ . No scaling parameters are necessary to provide an accurate fit for devices with different geometries.

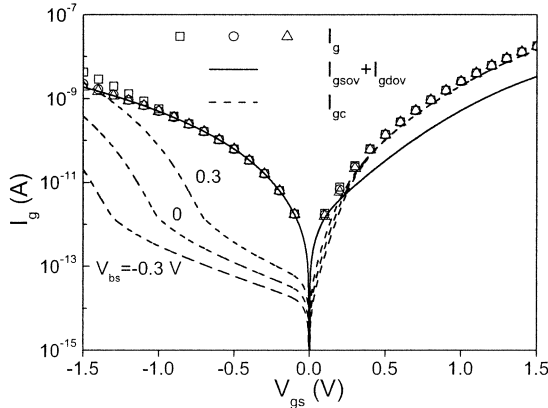


Figure 8: Decomposition of the total gate current into  $I_{gc}$  and  $I_{gsov} + I_{gdov}$  for the data shown in Fig. 6.

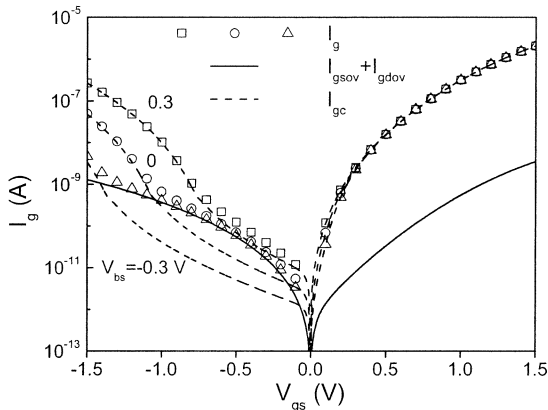


Figure 9: Decomposition of the total gate current into  $I_{gc}$  and  $I_{gsov} + I_{gdov}$  for the data shown in Fig. 7.

## 5 CONCLUSIONS

The new  $I_g$  model presented here is a part of a recently developed surface-potential-based compact MOSFET model (SP). However, it can be included in any other MOSFET model where the surface potential is available.

The increased physical content of the proposed model leads to high accuracy and physically meaningful results with a small number of adjustable parameters. Using symmetric linearization method, asymptotically correct partition of  $I_g$  into source and drain components is achieved in a closed form valid in all regions of operation.

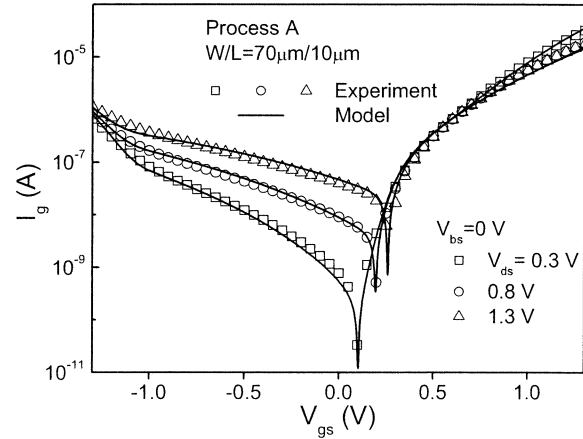


Figure 10: Experimental data for long-channel device by process A (symbols) and model calculations (lines) for different drain biases with  $V_{bs}=0$  V.

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